

# Package ‘patterncausality’

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**Type** Package

**Title** Pattern Causality Algorithm

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**Description** A comprehensive package for detecting and analyzing causal relationships in complex systems using pattern-based approaches. Key features include state space reconstruction, pattern identification, and causality strength evaluation.

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---

`AUCO`*Illapel Ecological Dataset*

---

**Description**

Raw rodent and rainfall data collected from the Las Chinchillas National Reserve near Illapel, Coquimbo Region of Chile. This dataset provides ecological time series for studying species interactions and environmental effects.

**Usage**`AUCO`**Format**

A data frame with rodent and rainfall data.

**Details**

Illapel Ecological Dataset

**Source**

Las Chinchillas National Reserve Research Station

**Examples**

```
data(AUCO)
head(AUCO)
summary(AUCO)
```

---

`climate_indices`*Climate Indices Dataset*

---

**Description**

A comprehensive time series dataset containing various climate indices used for pattern causality analysis. This dataset includes multiple climate indicators measured over time.

**Usage**`climate_indices`

**Format**

A data frame with 100 rows and 5 columns:

**Date** Date; Date of the measurement

**AO** Numeric; Arctic Oscillation index

**AAO** Numeric; Antarctic Oscillation index

**NAO** Numeric; North Atlantic Oscillation index

**PNA** Numeric; Pacific/North American index

**Details**

Climate Indices Dataset

**Source**

<https://www.cpc.ncep.noaa.gov/>

**Examples**

```
data(climate_indices)
head(climate_indices)
summary(climate_indices)
```

---

distanceMetric	<i>Distance Metric Interface</i>
----------------	----------------------------------

---

**Description**

A generic interface for computing distances between observations using either built-in or custom distance metrics.

**Usage**

```
distanceMetric(x, method = "euclidean", ...)

## Default S3 method:
distanceMetric(x, method = "euclidean", ...)

## S3 method for class 'custom'
distanceMetric(x, method, ...)
```

**Arguments**

x	Input data matrix or vector
method	Custom function to compute distances
...	Additional arguments passed to methods

**Details**

Generic Interface for Distance Metrics

**Value**

A distance object or matrix containing pairwise distances

**Methods (by class)**

- `distanceMetric(default)`: Default method using `stats::dist`
- `distanceMetric(custom)`: Custom distance metric implementation

**Examples**

```
## Not run:  
# Using default method  
x <- matrix(rnorm(100), ncol=2)  
d1 <- distanceMetric(x, "euclidean")  
  
# Using custom method  
custom_dist <- function(x) as.dist(crossprod(x))  
d2 <- distanceMetric(x, method=custom_dist)  
  
## End(Not run)
```

---

DJS

*Dow Jones Stock Price Dataset*

---

**Description**

A comprehensive dataset containing daily stock prices for 29 companies listed in the Dow Jones Industrial Average (DJIA). The dataset includes opening, closing, high, and low prices for each stock.

**Usage**

```
DJS
```

**Format**

A data frame with daily stock prices for 29 companies.

**Details**

Dow Jones Stock Price Dataset

**Source**

Yahoo Finance

**Examples**

```
data(DJS)
head(DJS)
summary(DJS)
```

---

```
optimalParametersSearch
```

*Search for Optimal Parameters in Pattern Causality Analysis*

---

**Description**

Searches for the optimal embedding dimension (E) and time delay (tau) to maximize the accuracy of causality predictions in a dataset. This function implements a grid search approach to evaluate different parameter combinations.

**Usage**

```
optimalParametersSearch(
  Emax,
  tauMax,
  metric = "euclidean",
  distance_fn = NULL,
  state_space_fn = NULL,
  dataset,
  h = 0,
  weighted = FALSE,
  relative = TRUE,
  verbose = FALSE
)
```

**Arguments**

Emax	Positive integer > 2; maximum embedding dimension to test
tauMax	Positive integer; maximum time delay to test
metric	Character string; distance metric for causality analysis ('euclidean', 'manhattan', 'maximum'). Defaults to "euclidean". Ignored if distance_fn is provided.
distance_fn	Optional custom distance function; takes two numeric vectors as input and returns a numeric distance. (default: NULL)
state_space_fn	Optional custom function for state space reconstruction; takes a numeric vector and parameters E and tau as input and returns a reconstructed state space. (default: NULL)
dataset	Numeric matrix; each column represents a time series.
h	Positive integer; prediction horizon.
weighted	Logical; if TRUE, weighted causality analysis is performed.

relative	Logical; if TRUE calculates relative changes ((new-old)/old), if FALSE calculates absolute changes (new-old) in signature space. Default is TRUE.
verbose	Logical; if TRUE, prints progress information. (default: FALSE)

### Details

#### Search for Optimal Parameters in Pattern Causality Analysis

This function evaluates each combination of embedding dimension and time delay for their effectiveness in detecting different types of causality:

- Total causality: Overall causal relationship strength
- Positive causality: Direct positive influences
- Negative causality: Direct negative influences
- Dark causality: Complex or indirect causal relationships

### Value

A pc\_params object containing:

- accuracy\_summary: A data frame summarizing the accuracy for each parameter combination.
- computation\_time: The time taken for the analysis.
- parameters: A list of the input parameters used.

### Examples

```
data(climate_indices)
dataset <- climate_indices[, -1]
optimalParams <- optimalParametersSearch(
  Emax = 3,
  tauMax = 3,
  metric = "euclidean",
  dataset = dataset,
  h = 1,
  weighted = FALSE
)
print(optimalParams)
```

### Description

Evaluates the causality prediction accuracy across multiple time series within a dataset using the PC Mk. II Light method. This function analyzes pairwise causality relationships and computes different types of causality measures.

**Usage**

```
pcAccuracy(
  dataset,
  E,
  tau,
  metric = "euclidean",
  h,
  weighted,
  distance_fn = NULL,
  state_space_fn = NULL,
  relative = TRUE,
  verbose = FALSE
)
```

**Arguments**

dataset	A matrix or data frame where each column represents a time series
E	Integer; embedding dimension for state space reconstruction ( $E > 1$ )
tau	Integer; time delay for state space reconstruction ( $\tau > 0$ )
metric	Character; distance metric to use, one of "euclidean", "manhattan", or "maximum"
h	Integer; prediction horizon, indicating forecast distance ( $h \geq 0$ )
weighted	Logical; whether to use weighted approach in calculating causality strengths
distance_fn	Optional custom distance function for computing distances (default: NULL)
state_space_fn	Optional custom function for state space reconstruction (default: NULL)
relative	Logical; if TRUE calculates relative changes $((\text{new-old})/\text{old})$ , if FALSE calculates absolute changes $(\text{new-old})$ in signature space. Default is TRUE.
verbose	Logical; whether to display progress information (default: FALSE)

**Details**

Calculate Pattern Causality Accuracy

**Value**

An object of class "pc\_accuracy" containing:

- parameters: List of input parameters (E, tau, metric, h, weighted)
- total: Mean total causality across all pairs
- positive: Mean positive causality across all pairs
- negative: Mean negative causality across all pairs
- dark: Mean dark causality across all pairs
- matrices: Raw causality matrices for each type



**See Also**

[pcMatrix](#) for analyzing individual causality matrices [pcLightweight](#) for pairwise causality analysis

**Examples**

```
data(climate_indices)
data <- climate_indices[, -1]
results <- pcAccuracy(dataset = data, E = 3, tau = 1,
                      metric = "euclidean", h = 1,
                      weighted = TRUE, verbose = TRUE)
print(results)
```

---

pcCrossMatrix

*Cross Pattern Causality Matrix Analysis*

---

**Description**

Analyzes pattern causality relationships between multiple time series in  $X$  and multiple time series in  $Y$  by computing pairwise causality measures and organizing them into a matrix.

**Usage**

```
pcCrossMatrix(
  X,
  Y,
  E,
  tau,
  metric = "euclidean",
  h,
  weighted = TRUE,
  distance_fn = NULL,
  state_space_fn = NULL,
  relative = TRUE,
  verbose = FALSE,
  n_cores = 1
)
```

**Arguments**

$X$	Matrix or data frame of time series for the cause
$Y$	Matrix or data frame of time series for the effect
$E$	Integer; embedding dimension
$\tau$	Integer; time delay

metric	Character; distance metric ("euclidean", "manhattan", "maximum")
h	Integer; prediction horizon
weighted	Logical; whether to use weighted causality
distance_fn	Optional custom distance function
state_space_fn	Optional custom state space reconstruction function
relative	Logical; if TRUE calculates relative changes ((new-old)/old), if FALSE calculates absolute changes (new-old) in signature space. Default is TRUE.
verbose	Logical; whether to print progress
n_cores	Integer; number of cores for parallel computation

### Details

Compute Cross Pattern Causality Matrix Analysis

The function performs these key steps:

- Validates input data and parameters
- Computes pairwise causality measures between X and Y
- Organizes results into a causality matrix
- Provides summary statistics for each causality type

### Value

A pc\_matrix object containing causality matrices

### Related Packages

- **vars**: Vector autoregression analysis
- **tseries**: Time series analysis tools
- **forecast**: Time series forecasting methods

---

pcCrossValidation

*Pattern Causality Cross-Validation Analysis*

---

### Description

Evaluates the robustness of pattern causality measures through repeated sampling analysis. This function performs cross-validation by analyzing multiple subsets of the data to assess the stability of causality relationships.

**Usage**

```
pcCrossValidation(
  X,
  Y,
  E,
  tau,
  metric = "euclidean",
  h,
  weighted,
  distance_fn = NULL,
  state_space_fn = NULL,
  numberset,
  random = TRUE,
  bootstrap = 1,
  verbose = FALSE,
  n_cores = 1,
  relative = TRUE
)
```

**Arguments**

X	Numeric vector representing the first time series.
Y	Numeric vector representing the second time series.
E	Integer specifying the embedding dimension.
tau	Integer specifying the time delay.
metric	Character string specifying the distance metric to use.
h	Integer specifying the prediction horizon.
weighted	Logical indicating whether to use weighted calculations.
distance_fn	Optional custom distance function.
state_space_fn	Optional custom state space function.
numberset	Numeric vector of sample sizes to analyze.
random	Logical indicating whether to use random sampling (default: TRUE).
bootstrap	Integer specifying the number of bootstrap iterations (default: 1).
verbose	Logical indicating whether to display progress messages.
n_cores	Integer specifying the number of cores to use for parallel computation (default: 1).
relative	Logical; if TRUE calculates relative changes ((new-old)/old), if FALSE calculates absolute changes (new-old) in signature space. Default is TRUE.

**Details**

Perform Pattern Causality Cross-Validation Analysis

The function implements these key steps:

- Validates input parameters and data
- Performs stratified sampling of time series data
- When random=TRUE and bootstrap>1, performs bootstrap sampling
- Computes pattern causality measures for each sample
- Aggregates results across all samples

When bootstrap sampling is enabled (random=TRUE and bootstrap>1), the function returns statistics including mean, 5% quantile, 95% quantile, and median for each sample size.

### Value

A `pc_cv` object containing:

- `samples`: Vector of sample sizes used
- `results`: Array of causality results
- `parameters`: List of analysis parameters

The results array structure depends on the bootstrap parameter:

- If `bootstrap>1`: A three-dimensional array where first dimension represents sample sizes, second dimension contains statistics (mean, quantiles, median), and third dimension represents causality types (positive, negative, dark)
- If `bootstrap=1`: A three-dimensional array where first dimension represents sample sizes, second dimension contains single values, and third dimension represents causality types (positive, negative, dark)

### See Also

[plot.pc\\_cv](#) for visualizing cross-validation results [print.pc\\_cv](#) for printing cross-validation results [summary.pc\\_cv](#) for summarizing cross-validation results

### Examples

```
data(climate_indices)
X <- climate_indices$A0
Y <- climate_indices$AA0

# Basic cross-validation
cv_result <- pcCrossValidation(
  X, Y,
  E = 3, tau = 1,
  metric = "euclidean",
  h = 1,
  weighted = FALSE,
  numberset = c(100, 200, 300)
)

# Cross-validation with bootstrap
cv_result_boot <- pcCrossValidation(
  X, Y,
```

```
E = 3, tau = 1,  
metric = "euclidean",  
h = 1,  
weighted = FALSE,  
numberset = c(100, 200, 300),  
random = TRUE,  
bootstrap = 100  
)
```

---

pcEffect

*Pattern Causality Effect Analysis*

---

### Description

Analyzes pattern causality matrices to compute and summarize the directional effects of different causality types (positive, negative, dark) between system components.

### Usage

```
pcEffect(pcmatrix, verbose = FALSE)
```

### Arguments

pcmatrix	An object of class "pc_matrix" containing causality matrices
verbose	Logical; whether to display computation progress (default: FALSE)

### Details

Calculate Pattern Causality Effect Analysis

The function performs these key steps:

- Processes raw causality matrices
- Computes received and exerted influence for each component
- Calculates net causality effect (difference between received and exerted)
- Normalizes results to percentage scale

### Value

An object of class "pc\_effect" containing:

- positive: Data frame of positive causality effects
- negative: Data frame of negative causality effects
- dark: Data frame of dark causality effects
- items: Vector of component names
- summary: Summary statistics for each causality type

### Related Packages

- **vars**: Vector autoregression for multivariate time series
- **lmtest**: Testing linear regression models
- **causality**: Causality testing and modeling

### See Also

[pcMatrix](#) for generating causality matrices [plot.pc\\_effect](#) for visualizing causality effects

### Examples

```
data(climate_indices)
dataset <- climate_indices[, -1]
pcmatrix <- pcMatrix(dataset, E = 3, tau = 1,
                     metric = "euclidean", h = 1,
                     weighted = TRUE)
effects <- pcEffect(pcmatrix)
print(effects)
plot(effects)
```

---

pcFullDetails

*Calculate Full Details Pattern Causality Analysis*

---

### Description

Implements an advanced pattern causality algorithm to explore the causal relationships between two time series datasets. This function provides comprehensive analysis of causality patterns, including state space reconstruction, pattern identification, and causality strength evaluation.

### Usage

```
pcFullDetails(
  X,
  Y,
  E,
  tau,
  h,
  weighted,
  metric = "euclidean",
  distance_fn = NULL,
  state_space_fn = NULL,
  relative = TRUE,
  verbose = FALSE
)
```

**Arguments**

X	Numeric vector; the first time series data
Y	Numeric vector; the second time series data
E	Integer; embedding dimension for state space reconstruction
tau	Integer; time delay between data points
h	Integer; prediction horizon for causality analysis
weighted	Logical; whether to weight causality strength
metric	Character; distance metric ('euclidean', 'manhattan', or 'maximum')
distance_fn	Optional custom distance function for computing distances (default: NULL)
state_space_fn	Optional custom function for state space reconstruction (default: NULL)
relative	Logical; if TRUE calculates relative changes ((new-old)/old), if FALSE calculates absolute changes (new-old) in signature space. Default is TRUE.
verbose	Logical; if TRUE, prints computation progress (default: FALSE)

**Details**

Calculate Full Details Pattern Causality Analysis

The function implements these key steps:

- State Space Reconstruction: Creates shadow attractors using embedding
- Pattern Analysis: Converts time series into signature and pattern spaces
- Nearest Neighbor Analysis: Identifies and analyzes local dynamics
- Causality Evaluation: Computes predicted and actual causality matrices
- Results Validation: Provides detailed diagnostics and quality metrics

**Value**

A `pc_full_details` object containing:

- `backtest_time`: Time points used for backtesting
- `valid_time`: Valid time points for analysis
- `causality_real`: Real causality spectrum
- `causality_pred`: Predicted causality spectrum
- `state_spaces`: State space reconstructions
- `neighbors`: Nearest neighbor information
- `patterns`: Pattern and signature information
- `matrices`: Causality matrices
- `predictions`: Predicted and actual values
- `weighted`: A logical indicating if weighted calculations were used
- `E`: Embedding dimension used for the analysis

---

pcLightweight

*Calculate Pattern Causality Using Lightweight Algorithm*


---

### Description

Implements a computationally efficient version of the Pattern Causality Model Mk. II for analyzing causal interactions between two time series. This function uses pattern and signature spaces to assess causality through reconstructed state spaces and hashed pattern analysis.

### Usage

```
pcLightweight(
  X,
  Y,
  E,
  tau,
  h,
  weighted,
  metric = "euclidean",
  distance_fn = NULL,
  state_space_fn = NULL,
  relative = TRUE,
  verbose = FALSE
)
```

### Arguments

X	A numeric vector representing the first time series
Y	A numeric vector representing the second time series
E	Integer; embedding dimension for state space reconstruction ( $E > 1$ )
tau	Integer; time delay for state space reconstruction ( $\tau > 0$ )
h	Integer; prediction horizon for future projections ( $h \geq 0$ )
weighted	Logical; whether to use weighted causality strength calculations
metric	Character string specifying the distance metric; one of "euclidean", "manhattan", or "maximum"
distance_fn	Custom distance function for state space reconstruction
state_space_fn	Custom function for state space transformation
relative	Logical; if TRUE calculates relative changes $((\text{new}-\text{old})/\text{old})$ , if FALSE calculates absolute changes $(\text{new}-\text{old})$ in signature space. Default is TRUE.
verbose	Logical; whether to display progress information (default: FALSE)



## Details

### Calculate Pattern Causality Using Lightweight Algorithm

The function implements these key steps:

- State space reconstruction using embedding parameters
- Pattern and signature space transformation
- Nearest neighbor analysis in reconstructed spaces
- Causality strength calculation using prediction accuracy
- Classification of causality types (positive/negative/dark)

## Value

An object of class "pc\_fit" containing:

- total: Total causality strength (0-1)
- positive: Proportion of positive causality (0-1)
- negative: Proportion of negative causality (0-1)
- dark: Proportion of dark causality (0-1)

## See Also

[pcFullDetails](#) for detailed analysis [pcMatrix](#) for analyzing multiple time series

## Examples

```
data(climate_indices)
X <- climate_indices$A0
Y <- climate_indices$AA0
result <- pcLightweight(X, Y, E = 3, tau = 1,
                       metric = "euclidean", h = 2,
                       weighted = TRUE, verbose = FALSE)

print(result)
summary(result)
plot(result)
```

## Description

Analyzes pattern causality relationships between multiple time series by computing pairwise causality measures and organizing them into matrices.

**Usage**

```
pcMatrix(
  dataset,
  E,
  tau,
  metric = "euclidean",
  h,
  weighted = TRUE,
  distance_fn = NULL,
  state_space_fn = NULL,
  relative = TRUE,
  verbose = FALSE,
  n_cores = 1
)
```

**Arguments**

dataset	Matrix or data frame of time series
E	Integer; embedding dimension
tau	Integer; time delay
metric	Character; distance metric ("euclidean", "manhattan", "maximum")
h	Integer; prediction horizon
weighted	Logical; whether to use weighted causality
distance_fn	Optional custom distance function
state_space_fn	Optional custom state space reconstruction function
relative	Logical; if TRUE calculates relative changes ((new-old)/old), if FALSE calculates absolute changes (new-old) in signature space. Default is TRUE.
verbose	Logical; whether to print progress
n_cores	Integer; number of cores for parallel computation

**Details**

Compute Pattern Causality Matrix Analysis

The function performs these key steps:

- Validates input data and parameters
- Computes pairwise causality measures
- Organizes results into causality matrices
- Provides summary statistics for each causality type

**Value**

A `pc_matrix` object containing causality matrices

**Related Packages**

- **vars**: Vector autoregression analysis
- **tseries**: Time series analysis tools
- **forecast**: Time series forecasting methods

---

pc\_cv

*Pattern Causality Cross-Validation Object*

---

**Description**

Creates a pattern causality cross-validation object containing results from repeated sampling analysis. This function constructs an object of class pc\_cv to store the results of cross-validation analysis.

**Usage**

```
pc_cv(samples = NULL, results = NULL, parameters = NULL)
```

**Arguments**

samples	Numeric vector of sample sizes used.
results	Matrix containing causality results for each sample.
parameters	List of analysis parameters.

**Value**

An object of class "pc\_cv".

---

pc\_effect

*Pattern Causality Effect Object*

---

**Description**

Creates a pattern causality effect object that contains information about the received and exerted influences for different causality types. This function constructs an object of class pc\_effect to store the results of effect analysis.

**Usage**

```
pc_effect(positive = NULL, negative = NULL, dark = NULL, items = NULL)
```

**Arguments**

positive	Data frame containing positive causality effects.
negative	Data frame containing negative causality effects.
dark	Data frame containing dark causality effects.
items	Names of items in the analysis.

**Value**

An object of class "pc\_effect".

---

pc_matrix	<i>Pattern Causality Matrix Object</i>
-----------	--

---

**Description**

Creates a pattern causality matrix object. This function constructs an object of class `pc_matrix` containing the positive, negative, and dark causality matrices, along with item names.

**Usage**

```
pc_matrix(
  positive = NULL,
  negative = NULL,
  dark = NULL,
  items = NULL,
  verbose = TRUE
)
```

**Arguments**

positive	Positive causality matrix.
negative	Negative causality matrix.
dark	Dark causality matrix.
items	Names of items in the matrices.
verbose	Logical, whether to print progress information.

**Value**

An object of class "pc\_matrix".

**Examples**

```
data(climate_indices)
dataset <- climate_indices[, -1]
pc_matrix_obj <- pcMatrix(dataset, E = 3, tau = 1,
  metric = "euclidean", h = 1, weighted = TRUE,
  verbose = FALSE)
print(pc_matrix_obj)
```

---

pc\_params *Pattern Causality Parameter Optimization Results*

---

**Description**

Creates an object containing parameter optimization results for pattern causality analysis

**Usage**

```
pc_params(accuracy_summary, computation_time, parameters)
```

**Arguments**

accuracy_summary	Data frame containing accuracy results for different parameter combinations
computation_time	Time taken for optimization
parameters	List of optimization parameters

**Details**

Pattern Causality Parameter Optimization Results

**Value**

An object of class "pc\_params"

---

plot.pc\_cv *Plot Pattern Causality Cross Validation Results*

---

**Description**

Visualizes the pattern causality cross-validation results. This function generates a line plot showing the causality strengths for different sample sizes.

**Usage**

```
## S3 method for class 'pc_cv'
plot(x, fr = FALSE, separate = FALSE, ...)
```

**Arguments**

x	A pc_cv object.
fr	Boolean for frame display.
separate	Boolean for separate plots.
...	Additional arguments passed to the plot function.

**Value**

Invisibly returns the input object.

**Examples**

```
data(climate_indices)
X <- climate_indices$A0
Y <- climate_indices$AA0
numbersets <- c(100, 150, 200)
cv_results <- pcCrossValidation(X, Y, 3, 2, "euclidean", 1, FALSE, numberset = numbersets)
plot(cv_results)
```

---

plot.pc\_effect

*Plot Pattern Causality Effect*


---

**Description**

Generates a plot to visualize the effects of positive, negative, or dark causality. Displays the influence exerted versus influence received for each item. This function generates a scatter plot showing the influence exerted versus influence received for each item, colored by the difference between exerted and received influence.

**Usage**

```
## S3 method for class 'pc_effect'
plot(
  x,
  status = "positive",
  add_label = TRUE,
  point_size = 3,
  label_size = 3,
  ...
)
```

**Arguments**

x	A pc_effect object.
status	Status of the effect to plot ("positive", "negative", or "dark").
add_label	Logical, whether to add labels to the plot.
point_size	Numeric value for point size (default: 3).
label_size	Numeric value for label text size (default: 3).
...	Additional arguments passed to plotting functions.

**Value**

Invisibly returns the ggplot object.

**Examples**

```

data(climate_indices)
dataset <- climate_indices[, -1]
pc_matrix_obj <- pcMatrix(dataset, E = 3, tau = 1,
  metric = "euclidean", h = 1, weighted = TRUE,
  verbose = FALSE)
effects <- pcEffect(pc_matrix_obj)
plot(effects, status = "positive")

```

---

plot.pc\_fit

*Plot Pattern Causality Results*


---

**Description**

Generates a combined plot of total causality and causality components for a `pc_fit` object. This function combines the visualizations from `plot_total` and `plot_components` into a single plot.

**Usage**

```

## S3 method for class 'pc_fit'
plot(x, ...)

```

**Arguments**

`x` A `pc_fit` object.

`...` Additional arguments passed to the underlying plotting functions.

**Value**

NULL invisibly.

---

plot.pc\_matrix

*Plot Pattern Causality Matrix*


---

**Description**

Creates a heatmap visualization of the pattern causality matrix for positive, negative, or dark causality relationships. This function generates a heatmap using `ggplot2` to visualize the specified causality matrix.

**Usage**

```
## S3 method for class 'pc_matrix'
plot(
  x,
  status,
  width = 0.85,
  height = 0.75,
  radius = grid::unit(3, "pt"),
  alpha = 0.53,
  show_text = FALSE,
  show_legend_title = FALSE,
  ...
)
```

**Arguments**

<code>x</code>	A <code>pc_matrix</code> object containing causality matrices.
<code>status</code>	The type of causality to plot ("positive", "negative", or "dark").
<code>width</code>	Numeric value specifying the width of the bars (default: 0.85).
<code>height</code>	Numeric value specifying the height of the bars (default: 0.75).
<code>radius</code>	Grid unit specifying the corner radius of the bars.
<code>alpha</code>	Numeric value specifying the transparency (default: 0.53).
<code>show_text</code>	Logical, whether to show numerical values on the plot.
<code>show_legend_title</code>	Logical, whether to display the legend title.
<code>...</code>	Additional arguments passed to plotting functions.

**Value**

A `ggplot` object invisibly.

**References**

Stavroglou et al. (2020) [doi:10.1073/pnas.1918269117](https://doi.org/10.1073/pnas.1918269117)

**Examples**

```
data(climate_indices)
dataset <- climate_indices[, -1]
pc_matrix_obj <- pcMatrix(dataset, E = 3, tau = 1,
  metric = "euclidean", h = 1, weighted = TRUE,
  verbose = FALSE)
plot(pc_matrix_obj, status = "positive")
```



---

plot.pc_state	<i>Plot State Space Reconstruction</i>
---------------	--

---

**Description**

Visualizes the state space reconstruction in 3D. This function generates a 3D scatter plot of the reconstructed state space.

**Usage**

```
## S3 method for class 'pc_state'
plot(x, style = 2, verbose = FALSE, ...)
```

**Arguments**

x	A pc_state object.
style	Integer; plot style (1 or 2).
verbose	Logical; whether to print verbose output.
...	Additional arguments passed to the plotting functions.

**Value**

Invisibly returns the input object.

---

plot_causality	<i>Plot Pattern Causality Time Series</i>
----------------	---

---

**Description**

Visualizes the positive, negative and dark causality components over time

**Usage**

```
plot_causality(x, type, ...)
```

**Arguments**

x	An object containing pattern causality results
type	The type of causality to plot ("total", "positive", "negative", or "dark")
...	Additional arguments passed to plotting functions

**Value**

Invisibly returns the ggplot object

---

plot\_causality.pc\_full\_details  
*Plot Pattern Causality Time Series*

---

**Description**

Visualizes the positive, negative and dark causality components over time

**Usage**

```
## S3 method for class 'pc_full_details'  
plot_causality(x, type, ...)
```

**Arguments**

x                    A pc\_full\_details object  
type                The type of causality to plot ("total", "positive", "negative", or "dark")  
...                 Additional arguments passed to plotting functions

**Value**

Invisibly returns the ggplot object

---

plot\_components        *Plot Pattern Causality Components*

---

**Description**

Visualizes the positive, negative, and dark causality components as a barplot. This function takes a pc\_fit object and generates a barplot showing the strength of each causality component.

**Usage**

```
plot_components(x, ...)
```

**Arguments**

x                    An object containing pattern causality results, typically a pc\_fit object.  
...                 Additional arguments passed to the underlying plotting functions.

**Value**

NULL invisibly.

**Examples**

```
data(climate_indices)
X <- climate_indices$A0
Y <- climate_indices$AA0
pc_result <- pcLightweight(X, Y, E = 3, tau = 2, metric = "euclidean", h = 1, weighted = TRUE)
plot_components(pc_result)
```

---

plot\_components.pc\_fit

*Plot Causality Components*


---

**Description**

Visualizes the positive, negative, and dark causality components as a barplot for a pc\_fit object. This function generates a barplot showing the strength of each causality component.

**Usage**

```
## S3 method for class 'pc_fit'
plot_components(x, ...)
```

**Arguments**

x                    A pc\_fit object.  
...                   Additional arguments passed to the underlying plotting functions.

**Value**

NULL.

---

plot\_total

*Plot Total Pattern Causality*


---

**Description**

Visualizes the total pattern causality strength as a barplot. This function takes a pc\_fit object and generates a barplot showing the overall causality strength.

**Usage**

```
plot_total(x, ...)
```

**Arguments**

x                    An object containing pattern causality results, typically a pc\_fit object.  
...                   Additional arguments passed to the underlying plotting functions.

**Value**

NULL invisibly.

**References**

Stavroglou et al. (2020) [doi:10.1073/pnas.1918269117](https://doi.org/10.1073/pnas.1918269117)

**See Also**

[plot\\_components](#) for visualizing individual causality components.

**Examples**

```
data(climate_indices)
X <- climate_indices$A0
Y <- climate_indices$AA0
pc_result <- pcLightweight(X, Y, E = 3, tau = 2, metric = "euclidean", h = 1, weighted = TRUE)
plot_total(pc_result)
```

---

plot\_total.pc\_fit      *Plot Total Causality*

---

**Description**

Visualizes the total causality strength as a barplot for a pc\_fit object. This function generates a barplot showing the total causality strength and its complement.

**Usage**

```
## S3 method for class 'pc_fit'
plot_total(x, ...)
```

**Arguments**

x                    A pc\_fit object.  
...                   Additional arguments passed to the underlying plotting functions.

**Value**

NULL.

---

print.pc\_accuracy      *Print Method for Pattern Causality Accuracy Results*

---

**Description**

Print Method for Pattern Causality Accuracy Results

**Usage**

```
## S3 method for class 'pc_accuracy'  
print(x, verbose = FALSE, ...)
```

**Arguments**

x	A pc_accuracy object
verbose	Logical; whether to display detailed information (default: FALSE)
...	Additional arguments passed to print

**Value**

Invisibly returns the input object

---

print.pc\_cv      *Print Pattern Causality Cross Validation Results*

---

**Description**

Prints the pattern causality cross-validation results. This function displays the parameters used for cross-validation, the sample sizes, and the summary statistics.

**Usage**

```
## S3 method for class 'pc_cv'  
print(x, ...)
```

**Arguments**

x	A pc_cv object.
...	Additional arguments passed to the print function.

**Value**

Invisibly returns the input object.

**Examples**

```

data(climate_indices)
X <- climate_indices$A0
Y <- climate_indices$AA0
numberset <- c(100, 150, 200)
cv_results <- pcCrossValidation(X, Y, 3, 2, "euclidean", 1, FALSE, numberset = numberset)
print(cv_results)

```

---

print.pc_effect	<i>Print Pattern Causality Effect</i>
-----------------	---------------------------------------

---

**Description**

Prints the pattern causality effect analysis results. This function displays the received and exerted influences for each item for positive, negative, and dark causality types.

**Usage**

```

## S3 method for class 'pc_effect'
print(x, ...)

```

**Arguments**

x	A pc_effect object.
...	Additional arguments passed to the print function.

**Value**

Invisibly returns the input object.

**Examples**

```

data(climate_indices)
dataset <- climate_indices[, -1]
pc_matrix_obj <- pcMatrix(dataset, E = 3, tau = 1,
  metric = "euclidean", h = 1, weighted = TRUE,
  verbose = FALSE)
effects <- pcEffect(pc_matrix_obj)
print(effects)

```

---

print.pc_fit	<i>Print Pattern Causality Results</i>
--------------	--

---

**Description**

Prints the pattern causality analysis results from a pc\_fit object. This function displays the total, positive, negative, and dark causality strengths.

**Usage**

```
## S3 method for class 'pc_fit'
print(x, ...)
```

**Arguments**

x	A pc_fit object.
...	Additional arguments passed to the print function.

**Value**

Invisibly returns the input object.

---

print.pc_matrix	<i>Print Pattern Causality Matrix</i>
-----------------	---------------------------------------

---

**Description**

Prints the pattern causality matrix object. This function displays the specified causality matrix (or all matrices) with a preview of the first 5 rows and columns.

**Usage**

```
## S3 method for class 'pc_matrix'
print(x, type = "all", ...)
```

**Arguments**

x	A pc_matrix object.
type	The type of matrix to print ("all" or "positive", "negative", "dark").
...	Additional arguments passed to the print function.

**Value**

Invisibly returns the input object.

**Examples**

```
data(climate_indices)
dataset <- climate_indices[, -1]
pc_matrix_obj <- pcMatrix(dataset, E = 3, tau = 1,
  metric = "euclidean", h = 1, weighted = TRUE,
  verbose = FALSE)
print(pc_matrix_obj, type = "positive")
```

---

print.pc\_params      *Print Method for Pattern Causality Parameter Results*

---

**Description**

Print Method for Pattern Causality Parameter Results

**Usage**

```
## S3 method for class 'pc_params'
print(x, verbose = FALSE, ...)
```

**Arguments**

x	A pc_params object
verbose	Logical; whether to display detailed information
...	Additional arguments passed to print

**Value**

Invisibly returns the input object

---

print.pc\_state      *Print State Space Reconstruction*

---

**Description**

Prints the state space reconstruction results. This function displays the parameters used for state space reconstruction and a preview of the reconstructed points.

**Usage**

```
## S3 method for class 'pc_state'
print(x, ...)
```



**Arguments**

x                    A pc\_state object.  
 ...                  Additional arguments passed to the print function.

**Value**

Invisibly returns the input object.

---

```
print.summary.pc_accuracy
```

*Print Method for Pattern Causality Accuracy Summary*

---

**Description**

Print Method for Pattern Causality Accuracy Summary

**Usage**

```
## S3 method for class 'summary.pc_accuracy'
print(x, ...)
```

**Arguments**

x                    A summary.pc\_accuracy object  
 ...                  Additional arguments passed to print

**Value**

Invisibly returns the input object

---

```
stateSpace
```

*State Space Reconstruction*

---

**Description**

Reconstructs the state space of a time series using delay embedding, creating a matrix where each row represents a point in the reconstructed space.

**Usage**

```
stateSpace(ts, E, tau, verbose = FALSE)
```

**Arguments**

ts	Numeric vector; time series data
E	Integer; embedding dimension ( $E > 1$ )
tau	Integer; time delay ( $\tau > 0$ )
verbose	Logical; whether to display progress information

**Details**

State Space Reconstruction Analysis

The function implements Takens' embedding theorem to reconstruct state space:

- Creates delay vectors using specified embedding dimension (E)
- Applies time delay (tau) between consecutive elements
- Handles boundary conditions and missing values

**Value**

An object of class "pc\_state" containing:

- matrix: The reconstructed state space matrix
- parameters: List of reconstruction parameters
- original: Original time series data

**Related Packages**

- **nonlinearTseries**: Nonlinear time series analysis
- **tseriesChaos**: Chaos theory analysis tools
- **fractal**: Fractal analysis methods

**Examples**

```
ts <- c(1:100)
result <- stateSpace(ts, E = 3, tau = 2)
plot(result)
```

---

stateSpaceMethod      *State Space Reconstruction Interface*

---

### Description

A generic interface for reconstructing state spaces from time series data using either built-in or custom methods.

### Usage

```
stateSpaceMethod(x, E, tau, ...)  
  
## Default S3 method:  
stateSpaceMethod(x, E, tau, ...)  
  
## S3 method for class 'custom'  
stateSpaceMethod(x, E, tau, method, ...)
```

### Arguments

x	Input time series
E	Embedding dimension (positive integer)
tau	Time delay (positive integer)
...	Additional arguments passed to methods
method	Custom function for state space reconstruction

### Details

Generic Interface for State Space Reconstruction

### Value

A list containing the reconstructed state space components

### Methods (by class)

- stateSpaceMethod(default): Default state space reconstruction
- stateSpaceMethod(custom): Custom state space reconstruction

### Examples

```
## Not run:  
# Using default method  
x <- rnorm(100)  
s1 <- stateSpaceMethod(x, E=3, tau=2)  
  
# Using custom method
```

```

custom_space <- function(x, E, tau) {
  list(matrix=embed(x, E))
}
s2 <- stateSpaceMethod(x, E=3, tau=2, method=custom_space)

## End(Not run)

```

---

summary.pc\_accuracy      *Summary Method for Pattern Causality Accuracy Results*

---

### Description

Summary Method for Pattern Causality Accuracy Results

### Usage

```

## S3 method for class 'pc_accuracy'
summary(object, ...)

```

### Arguments

object            A pc\_accuracy object  
...                Additional arguments passed to summary

### Value

A summary object for pc\_accuracy

---

summary.pc\_cv            *Summary of Pattern Causality Cross Validation Results*

---

### Description

Provides a summary of the pattern causality cross-validation results. This function calculates and displays summary statistics for the cross-validation results, including sample statistics, causality statistics, and convergence.

### Usage

```

## S3 method for class 'pc_cv'
summary(object, ...)

```

### Arguments

object            A pc\_cv object.  
...                Additional arguments passed to the summary function.

**Value**

Invisibly returns the input object.

**Examples**

```
data(climate_indices)
X <- climate_indices$A0
Y <- climate_indices$AA0
numberset <- c(100, 150, 200)
cv_results <- pcCrossValidation(X, Y, 3, 2, "euclidean", 1, FALSE, numberset = numberset)
summary(cv_results)
```

---

summary.pc\_effect

*Summarize Pattern Causality Effect*


---

**Description**

Provides a summary of the pattern causality effect analysis results. This function displays the summary statistics for the effects, including the number of components and the strongest effects.

**Usage**

```
## S3 method for class 'pc_effect'
summary(object, ...)
```

**Arguments**

`object`            A `pc_effect` object.  
`...`                Additional arguments passed to the `summary` function.

**Value**

Invisibly returns the input object.

**Examples**

```
data(climate_indices)
dataset <- climate_indices[, -1]
pc_matrix_obj <- pcMatrix(dataset, E = 3, tau = 1,
  metric = "euclidean", h = 1, weighted = TRUE,
  verbose = FALSE)
effects <- pcEffect(pc_matrix_obj)
summary(effects)
```

---

summary.pc_fit	<i>Summarize Pattern Causality Results</i>
----------------	--

---

**Description**

Provides a summary of the pattern causality analysis results from a `pc_fit` object. This function displays a table of causality strengths for total, positive, negative, and dark components.

**Usage**

```
## S3 method for class 'pc_fit'  
summary(object, ...)
```

**Arguments**

object	A <code>pc_fit</code> object.
...	Additional arguments passed to the summary function.

**Value**

Invisibly returns the input object.

---

summary.pc_matrix	<i>Summarize Pattern Causality Matrix</i>
-------------------	---

---

**Description**

Provides a summary of the pattern causality matrix object. This function calculates and displays descriptive statistics (mean, SD, min, max) for each causality matrix (positive, negative, dark).

**Usage**

```
## S3 method for class 'pc_matrix'  
summary(object, ...)
```

**Arguments**

object	A <code>pc_matrix</code> object.
...	Additional arguments passed to the summary function.

**Value**

Invisibly returns the input object.

**Examples**

```
data(climate_indices)
dataset <- climate_indices[, -1]
pc_matrix_obj <- pcMatrix(dataset, E = 3, tau = 1,
  metric = "euclidean", h = 1, weighted = TRUE,
  verbose = FALSE)
summary(pc_matrix_obj)
```

---

summary.pc_params	<i>Summary Method for Pattern Causality Parameter Results</i>
-------------------	---

---

**Description**

Summary Method for Pattern Causality Parameter Results

**Usage**

```
## S3 method for class 'pc_params'
summary(object, ...)
```

**Arguments**

object	A pc_params object
...	Additional arguments passed to summary

**Value**

A summary object for pc\_params

---

summary.pc_state	<i>Summarize State Space Reconstruction</i>
------------------	---

---

**Description**

Provides a summary of the state space reconstruction results. This function displays the dimensions, number of points, parameters, summary statistics for each dimension, and the number of missing values.

**Usage**

```
## S3 method for class 'pc_state'
summary(object, ...)
```

**Arguments**

object            A pc\_state object.  
...                Additional arguments passed to the summary function.

**Value**

Invisibly returns the input object.

---

validate\_custom\_fn\_output

*Validate Custom Function Output for Pattern Causality Analysis*

---

**Description**

Validates the Output Format from Custom Distance and State Space Functions to ensure compatibility with the package's internal processing.

**Usage**

```
validate_custom_fn_output(output, fn_name)
```

**Arguments**

output            The output from a custom function to validate  
fn\_name           The name of the function type being validated ("distance\_fn" or "state\_space\_fn")

**Details**

Validate Custom Function Output

**Value**

Nothing. Throws an error if validation fails.

**Examples**

```
# Example 1: Validating custom distance function output
custom_dist <- function(x) {
  # Create distance matrix
  dist_mat <- as.matrix(dist(x))
  # Validate output
  validate_custom_fn_output(dist_mat, "distance_fn")
  return(dist_mat)
}

# Example 2: Validating custom state space function output
custom_state_space <- function(x, E, tau) {
  # Create state space matrix
```



```
n <- length(x) - (E-1)*tau
state_mat <- matrix(nrow = n, ncol = E)
for(i in 1:E) {
  state_mat[,i] <- x[1:n + (i-1)*tau]
}
# Create output list
result <- list(matrix = state_mat,
               parameters = list(E = E, tau = tau))
# Validate output
validate_custom_fn_output(result, "state_space_fn")
return(result)
}

# Using the custom functions
x <- sin(seq(0, 4*pi, length.out = 100))
dist_result <- custom_dist(x)
space_result <- custom_state_space(x, E = 3, tau = 2)
```

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